A STUDY ON SOME GENERALISED UNIFORM SPACES IN THE CATEGORY C-TOP

A Thesis

Submitted in partial fulfillment

of the requirements for the completion of the degree

Ph.D in Mathematics.

Submitted by

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CHAPTER 7

CONCLUSION

7.1 Conclusion

In this thesis provides details on the core aspects of some generalisation of covering uniform structures viz, covering $L-$semi-uniform structure and covering $L-$ locally uniform structures in the $L-$Topological spaces in the category of **C-TOP**. They are studied in the context of other existing forms of generalised structures and in relation amongst themselves in attempt to provide a fairly complete framework consisting these generalised covering uniform structures.

In chapter 3, the notion of CLS-uniform space is introduced and various important uniform properties is investigated and some important results and their relation is given in the form of flowchart
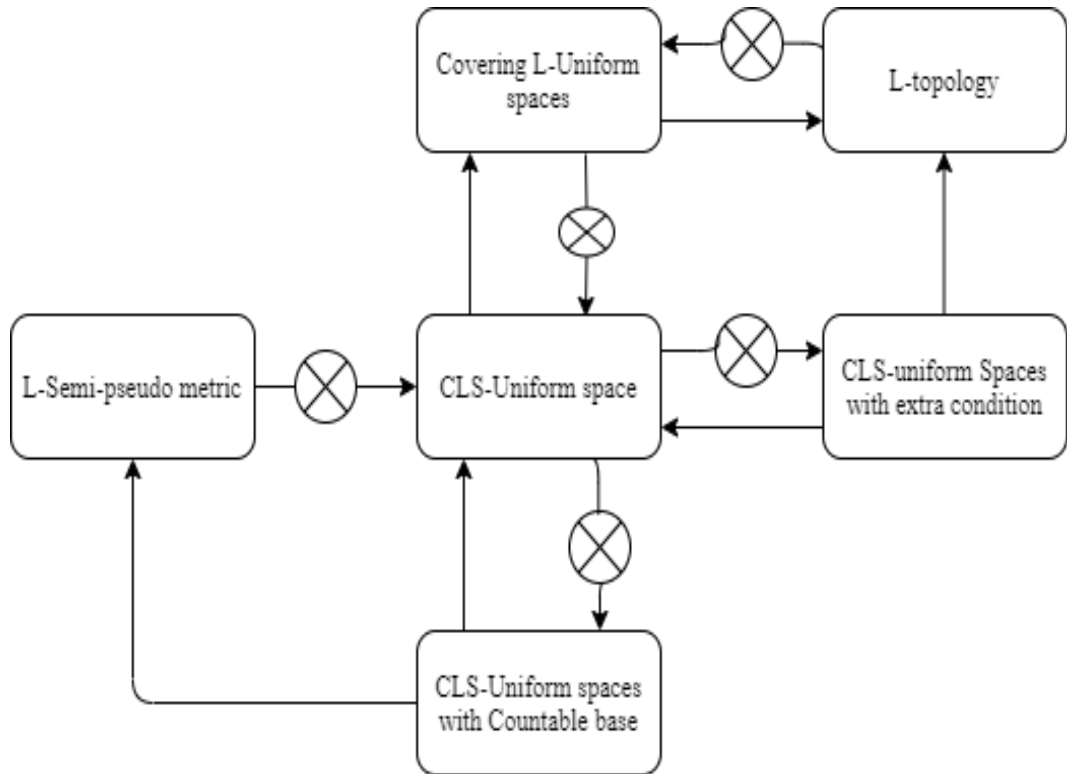
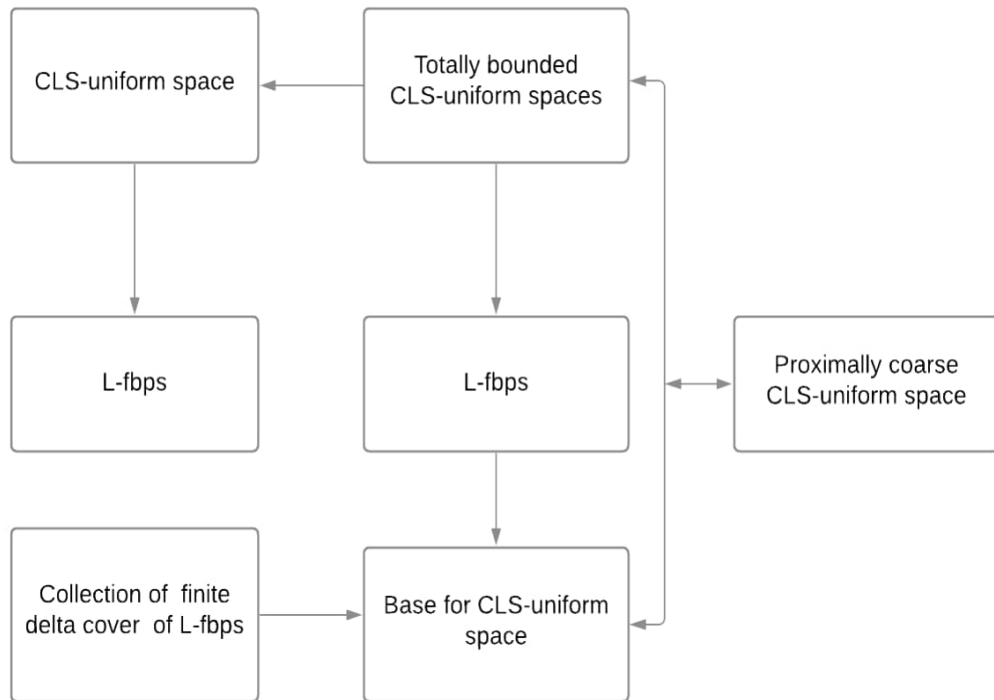**NB:** Meaning of the above symbols and subsequent flowcharts
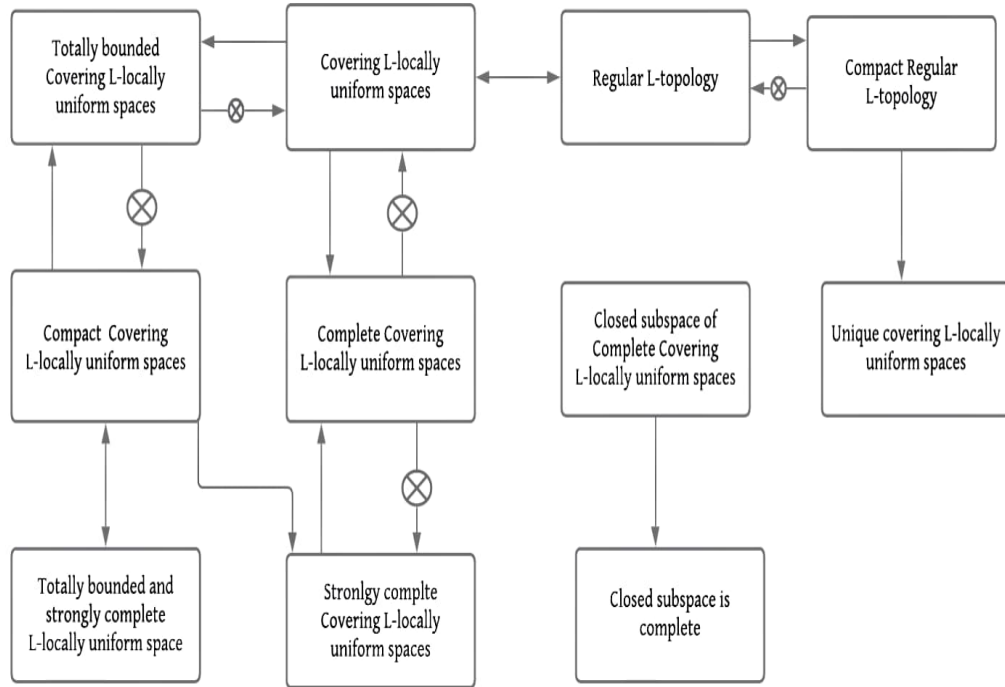
★ Implies

★ Does not implies

In chapter 4, the relation between the notion of CLS-uniform space and $L-$fuzzy basic proximity space and some important results and their relation is given in the form of flowchart

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┌──────────────────┐        ┌──────────────────┐
│                  │◄───────│  Totally bounded  │◄──┐
│ CLS-uniform space│        │ CLS-uniform spaces│   │
│                  │        │                  │   │
└────────┬─────────┘        └─────────┬────────┘   │
         │                            │            │
         ▼                            ▼            │
┌──────────────────┐        ┌──────────────────┐  │   ┌──────────────────┐
│                  │        │                  │  │   │  Proximally coarse│
│     L-fbps        │        │      L-fbps       │◄─┼──►│ CLS-uniform space │
│                  │        │                  │  │   │                  │
└──────────────────┘        └─────────┬────────┘  │   └──────────────────┘
                                      │            │
                                      ▼            │
┌──────────────────┐        ┌──────────────────┐  │
│ Collection of  finite│───►│ Base for CLS-uniform│─┘
│ delta cover  of L-fbps│    │       space        │
│                  │        │                  │
└──────────────────┘        └──────────────────┘
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In chapter 5, the notion of covering $L-$locally uniform space is introduced and various important uniform properties is investigated and some important results and their relation is given in the form of flowchart
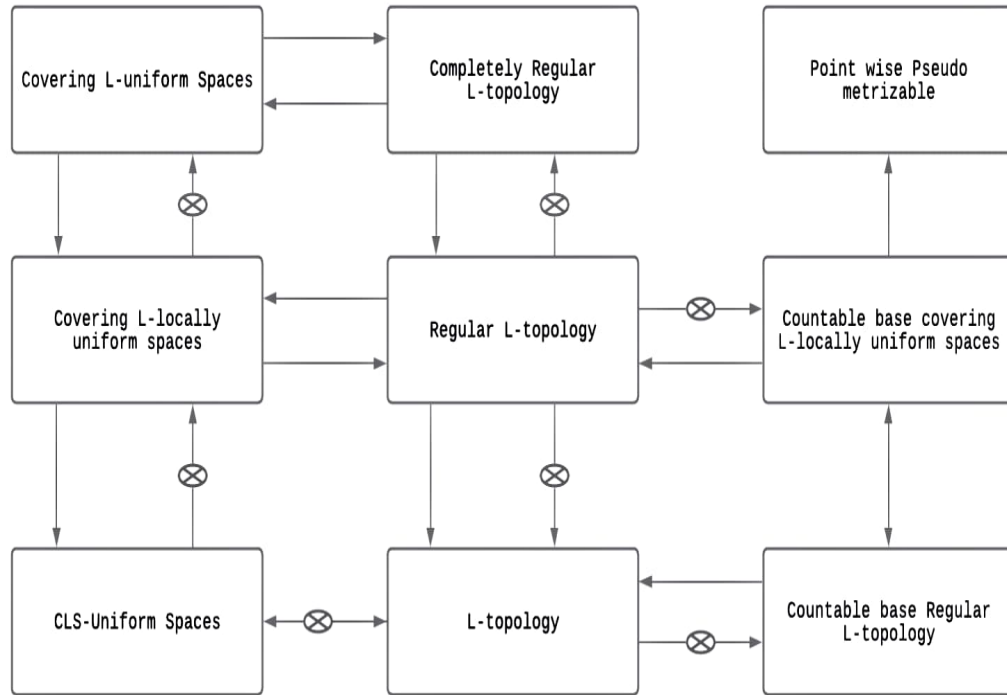
In chapter 6, the notion of further study on uniform properties is investigated in the context of covering $L-$locally uniform space, and some important results and their relation is given in the form of flowchart

Totally bounded Covering L-locally uniform spaces	Covering L-locally uniform spaces	Regular L-topology	Compact Regular L-topology

| Compact Covering L-locally uniform spaces | Complete Covering L-locally uniform spaces | Closed subspace of Complete Covering L-locally uniform spaces | Unique covering L-locally uniform spaces |

| Totally bounded and strongly complete L-locally uniform space | Stronlgy complte Covering L-locally uniform spaces | Closed subspace is complete | |

The findings of the thesis established that various uniform properties can be upgraded to a realistic degree using suitable existing notions, but also many new results can be generated in the broad perspective of covering generalised uniform structures.

The generalised covering uniform structures presented in this thesis are found to satisfy the following relation:

$$\text{Covering } L-\text{uniform space}$$

$$\Downarrow \nRightarrow$$

$$\text{Covering } L-\text{locally uniform spaces}$$

$$\Downarrow \nRightarrow$$

$$\text{CLS-uniform spaces}$$
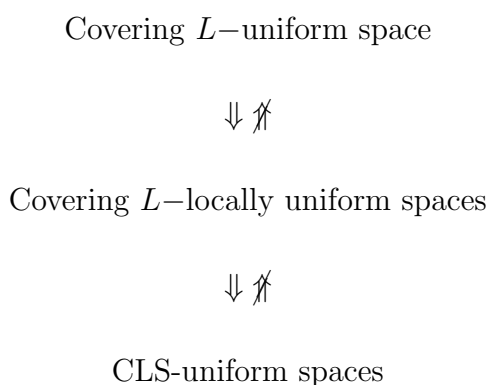
Various examples are provided to show that the converses are not true.

7.2   Future Research Scopes

The work carried out in this thesis opened up further study on different features of generalised covering uniform structures hat have been developed in this thesis. Briefly summarised further study directions, as follows-

• A study can carried out categoric classification comparison in various covering generalised uniform structures.

• A study of their application in various field of the context covering generalised uniform structures.

• A study can carry out relations between generalised covering uniform spaces relations with Merotopological Spaces.

• A study of uniformities related to algebraic structures in the context of covering generalised uniform structures.

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