

2018
ECONOMICS
ECO: 1.3
MATHEMATICAL ECONOMICS-I

Full Marks: 80
Time: 3 Hours

The figures in the margin indicates full marks for the questions :

1. Answer the following questions. **2x4=8**

- a. Explain integration as a reverse process of differentiation.
- b. What do you mean by absolute extrema?
- c. When does inverse of a matrix exist? What is adjoint of a matrix?
- d. What is pivot element?

2. Answer the following questions. **5x4=20**

- a. The AR function is given by
 $AR = 100 - 3q$, Find out the elasticity of demand when $q = 5$.
- b. Outline the properties of definite integrals
- c. Write down the general formulation of input-output analysis.
- d. Explain shortly the mathematical technique to find out pivot element in linear programming for a maximization problem.

3. Answer any two (2) of the following questions. **10x2=20**

- a. Analyze the effect of lump sum tax and Profit tax on profit, output and price of monopolist firm. (10)
- b. Explain producer's surplus mathematically. Assuming perfect competition, find producer's surplus from the demand and supply function given below (3+7)

$$p_d = 3x^2 - 20x + 5$$

$$p_s = 15 + 9x$$

- c. Find the demand vector D given; $X = \begin{matrix} 25 \\ 21 \\ 18 \end{matrix}$ $A = \begin{matrix} 0.2 & 0.3 & 0.2 \\ 0.4 & 0.1 & 0.2 \\ 0.1 & 0.3 & 0.2 \end{matrix}$ (10)

- d. Outline the general formulation of profit maximization for a production problem using LP technique. (10)

4. Answer the following questions.

16x2=32

A. A monopolist discriminates between two markets and the price equation are given below

$$P_1 = 80 - 5Q_1$$

$P_2 = 180 - 20Q_2$; Where Q_1 and Q_2 are the amount of output sold in two markets. The total cost function of the monopolist firm is given by $TC = 50 + 20Q$ where $Q = Q_1 + Q_2$. Obtain

- Profit Maximizing output
- Maximum profit
- Prices of the two markets
- Elasticity of demand of the two markets (6+2+4+4)

Or

B. Find the final output goals of each industry to satisfy the specified bill of final consumption. Given the technological coefficient matrix, find also the total labor requirement. (12+4)

	X	Y	Z	Bill of final consumption
X	0.3	0.2	0.2	80
Y	0.2	0.1	0.5	30
Z	0.2	0.4	0.2	50
Labour	0.4	0.3	0.1	

C. The Demand and supply laws are given by $D = (6-q)^2$ and $S = 14+q$ respectively. Find consumer's surplus if (i) the demand and supply are determined under pure competition (ii) the demand and supply are determined under monopoly. (8+8)

Or

D. What is linear programming? Elaborate the necessity of slack or dummy variables in solving profit maximization of a LP problem. A

manufacture produces three models of bicycles. The time in hours required for assembling, painting and packaging each model is as follows

	Model A	Model B	Model C
Assembling	2	2.5	3
Painting	1.5	2	1
Packaging	1	.75	1.25

The total time available for assembling, painting and packaging is 4006hrs, 2495hrs and 1500hrs respectively. The profit per model is Rs.45, Rs.50 and Rs.55 for models A, B and C respectively. How many of each type should be produced to obtain a maximum profit. (3+3+10)
