2022

(Held in 2023)

## **MATHEMATICS**

(Theory Paper)

Paper Code: MAT-305

## (Special Theory of Relativity)

Full Marks - 80

Pass Marks – 32

Time - Three hours

The figures in the margin indicate full marks for the questions.

- 1. Answer the following questions:  $1 \times 6 = 6$ 
  - (a) Distinguish between the inertial and non-inertial frame of reference.
  - (b) What is the fourth-coordinate according to Minkowski?
  - (c) Under which condition Lorentz transformation reduces to Galilean transformation?

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- (d) What is the mass of an object if it approaches the speed of light?
- (e) What is the resultant of two velocities of light each of which is less than c?
- (f) Length contraction happens in which direction?
- 2. Answer the following questions:  $2 \times 5 = 10$ 
  - (a) Which is invariant under Galilean transformation? What is the lowest possible mass of a particle?
  - (b) What are the postulates of the special theory of relativity?
  - (c) 'Simultaneity is not absolute' justify.
  - (d) What do you mean by Newtonian mechanics?
  - (e) Mention Maxwell's electromagnetic equations.
- 3. Answer any six from the following questions:  $5 \times 6 = 30$ 
  - (a) Establish the mass energy equivalence relation.
  - (b) Enunciate the variation of mass with velocity.
  - (c) Establish the Addition law of two velocities.
  - (d) Show that  $(ds)^2 = (dx)^2 + (dy)^2 + (dz)^2 (cdt)^2$  is invariant under Lorentz transformation.
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- (e) Give the geometrical interpretation of simultaneity, time dilation, length contraction.
- (f) Prove that laws of electromagnetism are not invariant under Galilean transformation.
- (g) If u and v are two velocities in the same direction and V is their resultant velocity given by

$$\tan^{-1}\frac{\mathbf{V}}{\mathbf{c}} = \tan^{-1}\frac{\mathbf{u}}{\mathbf{c}} + \tan^{-1}\frac{\mathbf{v}}{\mathbf{c}}$$

then deduce the law of composition of velocities from this equation.

- (h) Explain briefly about four vectors and four velocities.
- (i) Prove that Lorentz transformation forms a group.
- 4. Answer any *two* from the following questions:  $10 \times 2 = 20$ 
  - (i) What is Relativistic Lagrangian? Deduce Relativistic Lagrangian equations of motion.
  - (ii) Explain briefly about Minkowski space. Deduce relativistic equations of motion.
  - (iii) Discuss about invariance of Lorentz force equation.
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- 5. Answer any one of the following questions:  $14 \times 1 = 14$ 
  - (a) What is D'Alembert operator? Deduce the transformation equations for differential operator and prove that it is invariant under Lorentz transformations.
  - (b) Deduce the Lorentz transformations of electric field and magnetic field components and prove that Maxwell's equations are invariant under Lorentz transformations.