

2018
FORMAL LANGUAGE AND AUTOMATA THEORY
MCA :3.5
Full Marks: 75
Time: 3 Hours

*The figures in the margin indicates full marks for the questions :
(All Questions Are Compulsory)*

1. Answer the following:

1X10=10

- (i) The output of the Mealy machine depends on
- (a) the present state only
 - (b) the present state and the input symbol
 - (c) the input symbol only
 - (d) none of these
- (ii) The language accepted by PDA is
- (a) Type 0
 - (b) Type 1
 - (c) Type 2
 - (c) Type 3
- (iii) A Moorey Machine accepts a string w of length k. The length of the output string is
- (a) k+1
 - (b) k-1
 - (c) k
 - (d) k²
- (iv) The regular set denoted by the Regular Expression $(a+b)^+ (a+b)$ is
- (a) {a,b}
 - (b) {a,b,ab,ba}
 - (c) {aa,ab,ba,bb}
 - (d) {a,b,bb,aa}

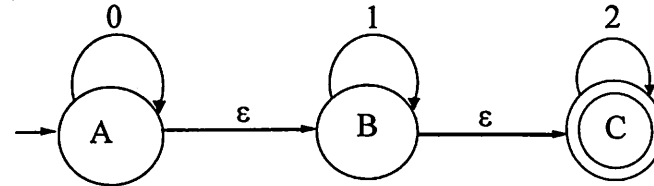
- (v) The Proof of Pumping Lemma is an example of
- iteration
 - recursion
 - Pigeon hole principle
 - all of the above
- (vi) A regular expression representing the language $\{\epsilon, a, b\}$ is
- $a+b$
 - ab
 - ϵab
 - $\epsilon + a+b$
- (vii) A regular expression $(0+1)(0+1)\dots\dots\dots(0+1)$ k times can be represented by a Finite Automata with
- exactly k states
 - exactly k+1 states
 - less than k states
 - cannot be determined
- (viii) The CFL $L = \{a^n b^n / n \geq 0\}$ can be generated by the following CFG
- $S \rightarrow \epsilon / ab / aSb$
 - $S \rightarrow ab / aSb$
 - $S \rightarrow \epsilon / aSb$
 - all of the above
- (ix) The Regular expression corresponding to CFG $S \rightarrow aS / bS / a / b$ is
- $a+b$
 - $(a+b)^*$
 - $(a+b)^*(a+b)$
 - none of the above
- (x) A Type 0 language is accepted by a
- Pushdown automata
 - Finite automata
 - Turing machine
 - none of the above

2. Answer the following:

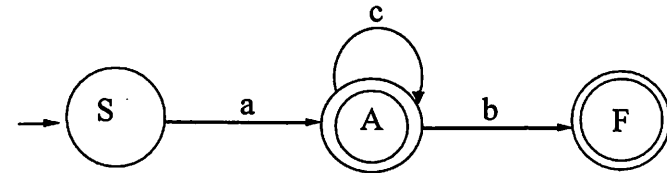
3X10=30

- (a) Show that the grammar $S \rightarrow a / abSb / aAb, A \rightarrow bS / aAAb$ is ambiguous.

- (b) Design a DFA for the set of strings over $\{a, b, \}$ odd no's of a's and odd no of b's.
- (c) Prove the following Identity- $\phi + R = R + \phi$
- (d) Find the following regular expression:
- the set of all strings containing at least 2a's over $\{a, b\}$
 - the set of strings over $\{0, 1\}$ containing alternate 0, s and 1's.
- (e) Construct a regular grammar G generating the regular set represented by $P = a^*b(a+b)^*$.
- (f) Construct a finite automata without null moves-



- (g) Describe the model of a PDA.
- (h) Construct a Finite Automata for the Regular Expression $(ab+c^*)^*bb$.
- (i) Find a Regular Expression corresponding to the following Finite Automata



- (j) Define Mealy and Moore machine.

3. Answer the following (Any five):

5X7=35

- Show that $L = \{0^i 1^j / i \geq 1\}$ is not regular.
- What is CNF? Find a grammar in CNF equivalent to $S \rightarrow aAbB, A \rightarrow aA/a, B \rightarrow bB/b$.

(c) Construct a PDA accepting $\{anbman / m,n \geq 1\}$ by null store. Construct the corresponding context-free grammar accepting the same set.

(d) If L is regular then LT is also regular.

(e) Find (i) Leftmost derivation and (ii) Rightmost derivation

for the string $aaababbba$ of Grammar G

$S \rightarrow aB / bA, A \rightarrow a/aS/bAA, B \rightarrow b/bS/aBB$

(f) Construct an equivalent DFA with reduced states equivalent to the Regular Expression $10 + (0 + 11)0^*1$.

(g) Define Chomsky Classification of Languages.

(h) construct a minimum state automaton equivalent to the finite automata from the given transition table:

State/ Σ	0	1
q_0	q_1	q_2
q_1	q_4	q_3
q_2^*	q_4	q_3
q_3^*	q_5	q_6
q_4	q_7	q_6
q_5	q_3	q_6
q_6	q_6	q_6
q_7	q_4	q_6
